STC/1/MAT/UG/2015

ESTD.1889

ST.THOMAS' COLLEGE
(AUTONOMOUS)
THRISSUR

Affiliated to

UNIVERSITY OF CALICUT

SYLLABUS FOR DEGREE OF

BACHELOR OF SCIENCE (B.Sc.)

IN

MATHEMATICS

(2015 onwards)

UNDERGRADUATE PROGRAMME – AN OVERVIEW

Programme means the entire course of study and examinations for the award of a degree. **Duration** of an undergraduate programme is six semesters distributed in a period of 3 years. An **academic week** is a unit of five working days in which distribution of work is organized from Monday to Friday with five contact periods of one hour duration on each day. A sequence of 18 such weeks (90 working days) constitutes a **semester**.

Course means a segment of subject matter to be covered in a semester. The undergraduate programme includes four types of courses, *viz.*, common courses, core courses, complementary courses and open course. **Common courses** include English and additional language courses. Every undergraduate student shall undergo 10 common courses [6 English courses and 4 additional language courses] for completing the programme. **Core courses** comprise compulsory course in a subject related to a particular degree programme offered by the parent department. There are 18 core courses including a project work. **Complementary courses** cover two disciplines that are related to the core subject and are distributed in the first four semesters. There shall be one **open course** in the 5th semester. Students can opt one open course of their choice offered by any department in the institution other than their parent department.

Each course shall have a unique alphanumeric **code number**, which includes abbreviation of the subject in three letters, the semester number (1 to 6) in which the course is offered, the code of the course (A: Common course, B: Core course, C: Complementary course and D: Open course) and the serial number of the course (01, 02, *etc.*). For example, MAT5B06 represents a core course of serial number 06 offered in 5th semester in B.Sc. Mathematics Programme.

Each course shall have certain credits. **Credit** is a unit of academic input measured in terms of weekly contact hours/course contents assigned to a course. For passing the degree programme, the students are required to achieve a minimum of **120 credits** as detailed below.

Common courses: 38 credits (22 for English courses + 16 for additional languages).

Core courses: 56 credits (including 2 credits for project work).

Complementary courses: 24 credits (12 credits each).

Open course: 2 credits.

Mark Distribution and Indirect Grading System

Mark system is followed instead of direct grading for each question. After external and internal evaluations marks are entered in the answer scripts. All other calculations, including grading, will be done by the university using the software. Indirect Grading System in 7 point scale is followed. Each course is evaluated by assigning marks with a letter grade (A^+, A, B, C, D, E or F) to that course by the method of indirect grading.

Mark Distribution

Sl. No.	*Course*	*Marks*
1	English	600
2	Additional Language	400
3	Core course: Mathematics	1350
4	Complementary course: Statistics	400
5	Complementary course: Physics or Computer Applications	400
6	Open Course	50
	Total Marks	**3200**

Seven point Indirect Grading System

% of Marks	*Grade*	*Interpretation*	*Grade Point Average*	*Range of Grade points*	*Class*
90 and above	A^+	Outstanding	6	5.5 - 6	First Class with distinction
80 to below 90	A	Excellent	5	4.5 – 5.49	
70 to below 80	B	Very good	4	3.5 – 4.49	First Class
60 to below 70	C	Good	3	2.5 – 3.49	
50 to below 60	D	Satisfactory	2	1.5 – 2.49	Second Class
40 to below 50	E	Pass/Adequate	1	0.5 – 1.49	Pass
Below 40	F	Failure	0	0 – 0.49	Fail

CORE COURSE THEORY: EVALUATION SCHEME

The evaluation scheme for each course contains two parts: *viz.,* internal evaluation and external evaluation.

1. INTERNAL EVALUATION

20% of the total marks in each course are for internal evaluation. The Departments shall send only the marks obtained for internal examination to the Controller of Examinations

Table 1: Components of Evaluation

Sl. No.	*Components*	*Marks*
1	Attendance	5
2	Test papers: I & II	5 + 5
3	Assignment	2
4	Seminar/ Viva*	3
	Total Marks	20

**Viva:* Open Course and Elective; *Seminar:* All Core and Complementary

Table 2: Percentage of Attendance and Eligible Marks

% of attendance	*Marks*
Above 90%	5
85-89%	4
80-84%	3
76-79%	2
75%	1

Table 3: Pattern of Test Papers

Duration	*Pattern*	*Total number of questions*	*Number of questions to be answered*	*Marks for each question*	*Marks*
1.5 Hours	One word	4	4	1	4
	Short answer	5	4	2	8
	Paragraph	5	3	6	18
	Essay	2	1	10	10
				*Total Marks**	40

* 36 Marks and above-5, 32 to 35- 4.5, 28 to 31 – 4, 24 to 27 – 3, 20 to 23 – 2, 14 to 19 – 1, Below 14 marks-0.

EXTERNAL EVALUATION

External evaluation carries 80% marks. Semestral examinations will be conducted at the end of each semester.

Pattern		Total No of Questions	No of questions to be answered	Marks for each question	Marks
A	One word	12	12	1	12
B	Short answer	12	9	2	18
C	Paragraph	9	6	5	30
D	Essay	3	2	10	20
				Total Marks	**80**

B.Sc. DEGREE PROGRAMME

MATHEMATICS (CORE COURSE)

DETAILS OF CORE COURSES

SL NO.	CODE	NAME OF THE COURSE	Semester	Marks	No. of Teaching Hours /Week	Credits
1	MAT1B01	Foundations of mathematics	I	100	4	4
2	MAT2B02	Calculus	II	100	4	4
3	MAT3B03	Calculus and analytic geometry	III	100	5	4
4	MAT4B04	Theory of equations, matrices and vector calculus	IV	100	5	4
5	MAT5B05	Vector calculus	V	100	5	4
6	MAT5B06	Abstract algebra	V	100	5	5
7	MAT5B07	Basic mathematical analysis	V	100	5	5
8	MAT5B08	Differential equations	V	100	5	4
9		Open Course (Offered by Other	V	50	3	2
10		Project/viva	V		2	---
11	MAT6B09	Real analysis	VI	100	5	5
12	MAT6B10	Complex analysis	VI	100	5	5
13	MAT6B11	Numerical methods	VI	100	5	4
14	MAT6B12	Number theory and linear algebra	VI	100	5	4
15	MAT6B13	Elective Course	VI	50	3	2
16	MAT6P14(PR)	Project/viva	VI	100	2	2
			Total	1400		

FIRST SEMESTER

MAT1B01: FOUNDATIONS OF MATHEMATICS

4 hours/week 4 credits

Syllabus

Text Books

1. S. Lipschutz: Set Theory and related topics (Second Edition), Schaum Outline Series, Tata McGraw-Hill Publishing Company, New Delhi.
2. Thomas /Finney : Calculus, 9th ed., LPE, Pearson Education.
3. K.H. Rosen: Discrete Mathematics and its Applications (sixth edition), Tata McGraw Hill Publishing Company, New Delhi.

Module 1 (16 hours)

Set theory

Pre-requisites: Sets, subsets, Set operations and the laws of set theory and Venn diagrams. Examples of finite and infinite sets. Finite sets and the counting principle. Empty set, properties of empty set (Quick review).

Syllabus:

Set operations, Difference and Symmetric difference, Algebra of sets, Duality, Classes of sets, Power sets (As in sections 1.6, 1.7 & 1.9 of Text book 1).

Relations: Product set, Relations (Directed graph of relations on set is omitted). Composition of relations, Types of relations, Partitions, Equivalence relations with example of congruence modulo relation, Partial ordering relations, n-ary relations. (As in Chapter 3 of text book 1 excluding 3.7).

Module II (16 hrs)

Functions

Pre-requisites: Basic ideas such as domain, co-domain and range of functions. Equality of functions, Injection, Surjection and Bijection(Quick review).

Syllabus: Identity function, constant functions, product (composition) of functions, theorems on one-one and onto functions, Mathematical functions, Recursively defined functions (As in Chapter 4 of text book 1). Indexed collection of sets, Operations on indexed collection of sets (As in 5.1, 5.2 and 5.3 of text book 1). Equipotent sets, Denumerable and countable sets, Cardinal numbers (Definitions and examples only as in 6.1, 6.2, 6.3 and 6.5 of text book 1)

Module III : (20hrs)

Function quick review , Shifting graphs , Limit and continuity , The Sandwich theorem, Target values and formal definition of limits, Extensions of limit concept, Continuity

(sections 3, 4, 1.1, 1.2, 1.3, 1.4 & 1.5 in text book 2)

Module IV (20 hrs)

Basic Logic

Pre-requisite: Nil.

Syllabus: Introduction, propositions, truth table, negation, conjunction and disjunction. Implications, biconditional propositions, converse, contra positive and inverse propositions and precedence of logical operators. Propositional equivalence: Logical equivalences. Predicates and quantifiers: Introduction, Quantifiers, Binding variables and Negations. (As in Chapter 1 of Text book 3).

References

1. P.R. Halmos: Naive Set Theory, Springer.

2. E. Kamke, Theory of Sets, Dover Publishers.

3. Anton : Calculus, Wiley.

4. R.P. Grimaldi: Discrete and Combinatorial Mathematics, Pearson Education.

SECOND SEMESTER

MAT2B02: CALCULUS

4 hours/week 4 credits

Syllabus

Text Books

1. Thomas / Finney : Calculus, 9th ed., LPE, Pearson Education.

Module I : (20 hrs)

Extreme value of functions, The mean value theorem, The first derivative test for local extremum values , Graphing with y' and y" , Limit as x → Assymptotes and dominant terms

(section 3.1, 3.2, 3.3, 3.4 & 3.5)

Module II (20 hrs)

Optimization, Linearization and differentials, Riemann sums and definite – integrals, Properties, area and the mean value theorem, The fundamental theorem, Substitution in Definite Integrals.

(section 3.6, 3.7, 4.5, 4.6, 4.7 & 4.8)

Module III (20 hrs)

Areas between curves, Finding volumes by slicing ,Volumes of solids of revolution (Disk method only), Lengths of plane curves, Areas of surface of revolution

(section5.1, 5.2, 5.3, 5.5 &5.6)

Module IV (12hrs)

Moments and centres of mass, Work
(section 5.7&5.8)

References:

1. Anton : Calculus, Wiley.

2. S.K. Stein : Calculus with Analytic Geometry, McGraw Hill.

THIRD SEMESTER

MAT3B03: CALCULUS AND ANALYTIC GEOMETRY

5 hours/week 4 credits

Syllabus

Text Books

1. Thomas / Finney : Calculus, 9th ed., LPE, Pearson Education.

Module I : Transcendental functions (15 hrs)

Natural logarithms, The Exponential function, and log , Growth and decay (quick review), L'Hopital's Rule, Relative rates of growth, Hyperbolic functions.

(section 6.2, 6.3, 6.4, 6.5, 6.6, 6.7, 6.10)

Module II – Infinite Series (25 hrs)

Limits of sequence of numbers, Theorems for calculating limits of sequences, Infinite series, Integral test for series of non-negative terms, Comparison test for series of non negative terms, Ratio and root test for series of non negative terms, Alternating series, Absolute and conditional convergence. (section 8.1, 8.2, 8.3, 8.4, 8.5, 8.6, 8.7)

Module III (15 hrs)

Power series, Taylor and Maclaurin's series, Convergence of Taylor series ,Error estimate

(section 8.8, 8.9, 8.10)

Module IV (35 hrs)

Conic section and quadratic equations, Classifying conic section by eccentricity ,Quadratic equations and rotations, Parametrisation of plane curves, Calculus with parametrised curves, Polar coordinates, Graphing in polar co-ordinates, Polar equations for conic sections, Integration in polar coordinates. (section 9.1, 9.2, 9.3, 9.4, 9.5, 9.6, 9.7, 9.8 &9.9)

References

1. Anton : Calculus, Wiley.

2. S.K. Stein : Calculus and Analytic Geometry, McGraw Hill.

FOURTH SEMESTER

MAT4B04: THEORY OF EQUATIONS, MATRICES AND VECTOR CALCULUS

5 hours/week 4credits

Syllabus

Text Books

1. Bernard and Child: Higher Algebra, Macmillan

2. Shanti Narayanan & Mittal : A Text Book of Matrices, Revised edn., S. Chand

3. Thomas /Finney : Calculus, 9th ed., LPE, Pearson Education.

Module I : Theory of Equations (30 hrs)

Polynomial Equations and Fundamental Theorem of Algebra(without proof). Applications of the Fundamental theorem to equations having one or more complex roots, Rational roots or multiple roots. Relations between roots and co-efficients of a polynomial equation and computation of symmetric functions of roots. Finding equations whose roots are functions of the roots of a given equation. Reciprocal equation and method of finding its roots. Analytical methods for solving polynomial equations of order up to four - quadratic formula. Cardano's method for solving cubic equations. Ferrari's method (for quadratic equations). Remarks about the insolvability of equations of degree five or more. Finding the nature of roots without solving Descartes' rule of signs.
(Sections from Text 1)

Module II: (16hrs)

Rank of a matrix – Elementary transformation, reduction to normal form, row reduced echelon form. Computing the inverse of a non singular matrix using elementary row transformation.

(Section 4.1 to 4.13 of Text 2)

Module III(20 hrs)

System of linear homogeneous equations. Null space and nullity of matrix. Sylvester's law of nullity. Range of a matrix. Systems of linear non homogeneous equations. Characteristic roots and characteristic vectors of a square matrix. Some fundamental theorem. Characteristic roots of Hermitian, Skew Hermitian and Unitary matrices. Characteristic equation of a matrix, Cayley-Hamilton theorem.

(Sections 6.1 to 6.6 and 11.1 to 11.3 and 11.11of Text 2)

Module IV (24 hrs)

(A quick review of Section 10.1 to 10.4)

Lines and planes in space. Cylinders and Quadric surfaces, Cylindrical and spherical coordinates, Vector valued functions and space curves, Arc length and Unit tangent vector , Curvature, torsion and TNB frame

(section10.5, 10.6, 10.7,11.1,11.3, 11.4 of text 3)

Reference

1.Kenneth Hoffman & Ray Kunze : Linear Algebra, Pearson Education.

2.ManicavachagomPillai, Natarajan, Ganapathy- Algebra

3.Dickson: First Course in Theory of Equation

4. Frank Ayres, Jr. : Matrices, Schaum's Outline Series, Asian Student edition.

5. Devi Prasad : Elementary Linear Algebra, Narosa Pub. House.

6. Kreyszig : Advanced Engineering Mathematics, 8th ed., Wiley.

7. H.F. Davis and A.D. Snider: Introduction to Vector Analysis, 6th ed.,

Universal Book Stall, New Delhi.

FIFTH SEMESTER

MAT5B05 : VECTOR CALCULUS

5 hours/week 4 credits

Syllabus

Text Books : Thomas / Finney : Calculus, 9th ed., LPE, Pearson Education.

Module I (15 hrs)

Functions of several variables ,Limits and Continuity , Partial derivatives , Differentiability linearization and differentials, Chain rule, Partial derivatives with constrained variables

(section 12.1, 12.2, 12.3, 12.4, 12.5, 12.6)

Module II – Multivariable functions and Partial Derivatives (20 hrs)

Directional derivatives, gradient vectors and tangent planes , Extreme value and saddle points, Lagrange multipliers , Taylor's formula, Double Integrals , Double integrals in polar form

(section 12.7, 12.8, 12.9, 12.10, 13.1, 13.3)

Module III (25 hrs)

Triple integrals in Rectangular Coordinates , Triple integrals in cylindrical and spherical co-ordinates, Substitutions in multiple integrals, Line integrals , Vector fields, work circulation and flux , Path independence, potential functions and conservative fields (section 13.4, 13.6, 13.7, 14.1, 14.2, 14.3)

Module IV – Integration in Vector Fields (30 hours)

Green's theorem in the plane , Surface area and surface integrals, Parametrized surfaces, Stokes' theorem (statement only) , Divergence theorem and unified theory (no proof). (section14.4, 14.5, 14.6, 14.7, 14.8)

References

1. Kreyszig : Advanced Engineering Mathematics, 8th ed., Wiley.

2. H.F. Davis and A.D. Snider: Introduction to Vector Analysis, 6th ed.,

Universal Book Stall, New Delhi.

FIFTH SEMESTER

MAT5B06 : ABSTRACT ALGEBRA

5 hours/week 5 credits

Text Books:

1. John B. Fraleigh : A First Course in Abstract Algebra, 7th Ed., Pearson.

Module I (20 hrs)

Binary operations; Isomorphic binary structures; Groups; Sub groups

(Sections 2, 3, 4 & 5).

Module II (25 hrs)

Cyclic groups; Groups and permutations; Orbits, cycles and Alternating groups

(Sections 6, 8 & 9).

Module III (15 hrs)

Cosets and Theorem of Lagrange; Homomorphisms

(Sections 10 & 13).

Module IV (30 hrs)

Rings and Fields; Integral Domains, The Field of Quotients of an Integral Domain

(Sections 18, 19 & 21).

References

1. Joseph A. Gallian : Contemporary Abstract Algebra. Narosa Pub. House.

2. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul: Basic Abstract Algebra, 2nded., Cambridge University Press.

3. Artin : Algebra, PHI.

6. Durbin : Modern Algebra : An Introduction, 5th ed., Wiley.

FIFTH SEMESTER

MAT5B07 : BASIC MATHEMATICAL ANALYSIS

5 hours/week 5 credits

Text 1 : Robert G. Bartle & Donald R. Sherbert : Introduction to Real Analysis, 3rd ed., Wiley.

Text 2 : J.W. Brown and Ruel V. Churchill : Complex Variables and Applications, 8th Ed., McGraw Hill.

Module I (20 hrs)

A quick review of sets and functions ,Mathematical induction ,Finite and infinite sets

Real Numbers ,The algebraic property of real numbers

(Sec. 1.1, 1.2, 1.3, 2.1 of text 1)

Module II (20 hrs)

Absolute value and real line ,The completeness property of R ,Applications of supremum property

Intervals, Nested interval property and uncountability of R

(Sec 2.2, 2.3, 2.4 and 2.5 of text 1)

Module III (30 hrs)

Sequence of real numbers, Sequence and their limits, Limit theorems, Monotone sequences

Subsequence and Bolzano – Weirstrass theorem, Cauchy criterio, Properly divergent sequences.

Open and closed sets

(Sec. 3.1, 3.2, 3.3, 3.4, 3.5, 3.6 and 11.1 of text 1)

Module IV : Complex Numbers (20 hrs)

Sums and Products; Basic Algebraic properties; Further properties, Vectors and Moduli; Complex conjugates; Exponential form; Product and powers in exponential form; Arguments of products and quotients; Roots of complex numbers; Regions in the complex plane.

(Sections 1 to 11 of Chapter 1 of Text 2)

References

1. J.M. Howie : Real Analysis, Springer 2007.

2. Ghorpade and Limaye : A Course in Calculus and Real Analysis, Springer, 2006.

3. K.A. Ross : Elementary Real Analysis : The Theory of Calculus, Springer Indian Reprint.

4. J.V. Deshpande : Mathematical Analysis and Applications, Narosh Pub. House.

5. M.R. Spiegel : Complex Variables, Schaum's Outline Series.

FIFTH SEMESTER

MAT5B08 : DIFFERENTIAL EQUATIONS

5 hours/week 4 credits

Text Book :

W.E. Boyce & R.C. Diprima, Elementary Differential Equations and Boundary Value Problems. John Wiley & Sons, 7th Edn.

Module I (24 hrs)

(a) Introduction, Some Basic Mathematical Models; Direction Fields, Solutions of some Differential equations, Classification of Differential Equations, Historical Remarks.

(Chapter 1, Sec. 1.1.1.2, 1.3, 1.4)

(b) First order differential equations

Linear equations with variable coefficients , Separable equations, Modeling with first order equations , Differences between linear and non linear equations, Exact equations and integrating factors , The existence and uniqueness theorem (proof omitted)

(Chapter 2 – Sec. 2.1, 2.2, 2.3, 2.4, 2.6, 2.8)

Module II (29 hrs)

(a) Second Order Linear Differential Equations

Homogeneous equation with constant coefficients, Fundamental solutions of Linear Homogeneous equations, Linear independence and Wronskian, Complex roots of characteristic equations, Repeated roots; Reduction of order, Non homogeneous equations; Method of Undetermined coefficients, Variation of parameters, Mechanical and Electrical vibrations(upto and including e.g. 1)

(Chapter 3 – Sec. 3.1 to 3.8)

(b) Systems of First Order Linear equations

Introduction , Basic theory of systems of first order Linear Equations

(Chapter 7 – Sec. 7.1, 7.4)

Module III : Laplace Transforms (17 hrs)

Definition of Laplace Transforms , Solution of Initial Value Problem , Step functions , Impulse functions, The Convolution Integral

(Chapter 6 – Sec. 6.1, 6.2, 6.3, 6.5, 6.6)

Module IV : Partial Differential Equations and Fourier Series (20 hrs)

Two point Boundary value problems , Fourier Series, The Fourier Convergence Theorem

Even and odd functions , Separation of variables; Heat conduction in a rod , The Wave equation: Vibrations of an elastic string

(Chapter 10 – Sec. 10.1, 10.2, 10.3, 10.4, 10.5, 10.7)

References

1. S.L. Ross : Differential Equations, 3rd ed., Wiley.

2. A.H. Siddiqi & P. Manchanda : A First Course in Differential Equation with Applications, Macmillan, 2006.

3. E.A. Coddington : An Introduction to Ordinary Differential Equation, PHI.

4. G.F. Simmons : Differential Equation with Application and Historical Notes, Second ed.

5. M. Braun : Differential Equations and their Applications, Springer.

SIXTH SEMESTER

MAT6B09 : REAL ANALYSIS

5 hours/week 5 credits

Text :

1. G. Bartle, Donald R. Sherbert : Introduction to Real Analysis (3rd Edn.)

2. R.R. Goldberg : Methods of Real Analysis.

3. Narayanan& Manicavachagom Pillay : Calculus, Vol. II

Module I : Continuous Functions (25 hrs)

Continuous functions (a quick review), Continuous functions on intervals , Uniform continuity

(Sec. 5.3, 5.4 of text 1)

Module II : Riemann Integral (25 hrs)

Riemann Integral , Riemann Integrable Functions , The fundamental theorem , Substitution theorem and application, Approximate Integration

(Sec. 7.1, 7.2, 7.3, 7.4 of text 1)

Module III : Sequence and series of functions (20 hrs)

A quick review of series of real numbers, Pointwise and uniform convergence, Interchange of limit and continuity, Series of functions .

(8.1, 8.2.1, 8.2.2, 9.4.1, 9.4.2, 9.4.5, 9.4.6 of text 1)

Module IV (20 hrs)

Improper Integrals

Improper integrals of the first kind, Improper integrals of the second kind, Cauchy Principal value, Improper Integrals of the third kind.

(Sections: 7.9, 7.10 of text 2)

Beta and Gamma functions

Beta Functions, Gamma Functions, Relation between Beta and Gamma Functions

(Chapter IX, Sec: 2.1, 2.2, 2.3, 3, 4, 5 of text 3)

References

1. J.V. Deshpande: Mathematical Analysis and Applications, Narosa Pub. House.

2. TorenceTao : Analysis I, TRIM 37, Hindustan Book Agency.

3. K.A. Ross: Elementary Real Analysis : Theory of Calculus, Springer.

4. K.G. Binmore: Mathematical Analysis, CUP.

SIXTH SEMESTER

MAT6B10 : COMPLEX ANALYSIS

5 hours/week 5credits

Text : James Ward Brown and Ruel V. Churchill : Complex Variables and Applications (8th Edn.), McGraw Hill.

Module I : Analytic Functions (24 hrs)

Functions of complex variable, Limits Theorems on limits, Limits involving the points at infinity, Continuity derivatives, Differentiation formula, Cauchy-Riemann Equations, Polar coordinates, Analytic functions, Harmonic functions

(Sec: 12, 15 to 26 of Chapter 2)

Elementary functions

The exponential function, Logarithmic function, Complex exponents, Trigonometric functions, Hyperbolic functions, Inverse Trigonometric and Hyperbolic functions.

(Sec. 29 to 36 of Chapter 3)

Module II : Integrals (22 hrs)

Derivatives of functions $\omega(t)$; Indefinite integral of $\omega(t)$; Contours, Contour integrals, Antiderivatives, Cauchy-Goursat theorem (without proof), Simply and multiply connected domains, Cauchy's integral formula and its extension, Liouville's theorem and fundamental theorem of algebra, Maximum modulus principle.

(Sec: 37 to 54 excluding 42, 47 of Chapter 4)

Module III : Series (22 hrs)

A quick review of convergence of sequence and series of complex numbers.

Taylor series, Laurents series (without proof), Applications.

Power series: Absolute and uniform convergence. Continuity of sum of power series, Differentiation and integration of power series, Multiplication and division of power series.

(Sec: 55 to 60 & 62 to 67 of Chapter 5). 28

Module IV : Residues (22 hrs)

Isolated singular points, Residues, Cauchy's residue theorem, Residue at infinity, Three types of isolated singular points, Residues at poles, Zeroes of analytic functions, Zeroes and poles.

(Sec: 68 to 76 of Chapter 6).

Applications of residues

Evaluation of improper integrals, Jordan's Lemma (statement only), Definite integrals involving sines and cosines.

(Sec: 78, 79, 80 and 85 of Chapter 7).

References

1. Mark J.Ablowitz and Anthanassios S. Fokas: Complex Variables, Cambridge Text, 2nd Edn.
2. S. Ponnusamy : Foundation of Complex Analysis : Narosa.
3. Murray R. Spiegel: Complex Variables, Schaum's Outline series.
4. J.M. Howie: Complex Analysis: Springer India Reprint.
5. Stewart & Tall: Complex Analysis, CUP

SIXTH SEMESTER

MAT6B11 : NUMERICAL METHODS

5 hours/week 4 credits

Text :

S.S. Sastry : Introductory Methods of Numerical Analysis, Fourth Edition, PHI.

Module I : Solution of Algebraic and Transcendental Equation (23 hrs)

2.1 Introduction, 2.2 Bisection Method, 2.3 Method of false position, 2.4 Iteration method

2.5 Newton-Raphson Method, 2.6 Ramanujan's method , 2.7 The Secant Method ,

Finite Differences

3.1 Introduction , 3.3.1 Forward differences , 3.3.2 Backward differences , 3.3.3 Central differences

3.3.4 Symbolic relations and separation of symbols , 3.5 Differences of a polynomial

Module II : Interpolation (23 hrs)

3.6 Newton's formulae for intrapolation, 3.7 Central difference interpolation formulae , 3.7.1 Gauss' Central Difference Formulae , 3.9 Interpolation with unevenly spaced points , 3.9.1 Langrange's interpolation formula , 3.10 Divided differences and their properties , 3.10.1 Newton's General interpolation formula ,3.11 Inverse interpolation ,

Numerical Differentiation and Integration

5.1 Introduction , 5.2 Numerical differentiation (using Newton's forward and backward formulae)

5.4 Numerical Integration , 5.4.1 Trapizaoidal Rule , 5.4.2 Simpson's 1/3-Rule , 5.4.3 Simpson's 3/8-Rule

Module III : Matrices and Linear Systems of equations (22 hrs)

6.3 Solution of Linear Systems – Direct Methods , 6.3.2 Gauss elimination , 6.3.3 Gauss-Jordan Method, 6.3.4 Modification of Gauss method to compute the inverse , 6.3.6 LU Decomposition, 6.3.7 LU Decomposition from Gauss elimination

6.4 Solution of Linear Systems – Iterative methods , 6.5 The eigen value problem , 6.5.1 Eigen values of Symmetric Tridiazonal matrix

Module IV : Numerical Solutions of Ordinary Differential Equations (22 hrs)

7.1 Introduction , 7.2 Solution by Taylor's series , 7.3 Picard's method of successive approximations , 7.4 Euler's method , 7.4.2 Modified Euler's Method, 7.5 Runge-Kutta method

7.6 Predictor-Corrector Methods , 7.6.1 Adams-Moulton Method , 7.6.2 Milne's method

References

1. S. Sankara Rao : Numerical Methods of Scientists and Engineer, 3rd ed., PHI.

2. F.B. Hidebrand : Introduction to Numerical Analysis, TMH.

3. J.B. Scarborough : Numerical Mathematical Analysis, Oxford and IBH

SIXTH SEMESTER

MAT6B12 : NUMBER THEORY AND LINEAR ALGEBRA

5 hours/week 4 credits

Text Books:

1. David M. Burton : Elementary Number Theory, Sixth Edn., TMH.

2. T. S. Blynth and E.F. Robertson: Basic Linear Algebra, second Edn springer under graduate mathematics series 2009

Module I – Theory of Numbers (30 hrs)

Divisibility theory in the integers – the division algorithm, the greatest common divisor, the Euclidean algorithm, the Diophantine equation ax + by = c. Primes and their distribution. The fundamental theorem of arithmetic. The sieve of Eratosthenes. The theory of congruences. Basic properties of congruence. Binary and decimal representation of integers. Linear congruences and Chinese remainder theorem.

(Sections 2.2, 2.3, 2.4, 2.5, 3.1, 3.2, 4.2, 4.3 & 4.4 of Text 1).

Module II (25 hrs)

Fermat's little theorem and pseudoprimes Wilson's theorem. The sum and number of divisors. The greatest integer function. Euler's phi-function. Euler's generalization of Fermat's theorem. Properties of the phi-function.

(Sections 5.2, 5.3, 6.1, 6.3, 7.2, 7.3 and 7.4 of Text 1) (Theorems 7.6 and 7.7 only).

Module III (15 hrs)

Vectorspaces - examples, linear combinations, spanning, linear independence, base, finite dimensional vector spaces

(All Sections in chapter 5 of text 2)

Module IV (20 hrs)

Linear mappings- Linear transformations, examples, nullspace, rank –nullity theorem, linear isomorphism.

(All Sections in chapter 6 of text 2)

References

1. C.Y. Hsiung : Elementary Theory of Numbers. Allied Publishers.

2. Neville Robbins : Beginning Number Theory, Second Ed. Narosa.

3. George E. Andrews : Number Theory, HPC.

4. Kenneth Hoffman & Ray Kunze : Linear Algebra, Pearson Education.

5. Frank Ayres, Jr. : Matrices, Schaum's Outline Series, Asian Student edition.

6. Devi Prasad : Elementary Linear Algebra, Narosa Pub. House.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (ELECTIVE COURSE)

SIXTH SEMESTER

B.Sc. DEGREE PROGRAMME
MATHEMATICS (ELECTIVE COURSE)
SIXTH SEMESTER

MAT6B13(E02) : LINEAR PROGRAMMING

3 hours/week **2 credits**

Text Book : Gupta and Manmohan - Linear Programming And Theory of Games

MODULE 1:

Formulation, Convex sets, General LLP
(Section 0.4, 1..6, 1.7 , 1..8, chapter 2, chapter 3)

MODULE 2:

Simplex Method, Duality
(Section 4.6, 5.1, 5.2, 5.3, 5.4, 6.1, 6.2, 6.3, 6.4 (Theorem 1)

MODULE 3 :

The transportation problem, The assignment Problems
(Section 11.1 to 11-.11, 11.14, 12.1 to 12.4 |

References

1. K. V. Mital & Manmohan: Optimization methods in Operations Research and Systems Analysis, 3rd Edn., New Age International publishers.
2. Dipak Chatterjee: Linear Programming and Game Theory, Prentice Hall of India.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (OPEN COURSE)

FIFTH SEMESTER

(For students not having Mathematics as Core Course)

MAT5D17: MATHEMATICS FOR PHYSICAL SCIENCES

3 hours/week **2 credits**

Text Book:

1. John B Fraleigh : A First Course in Abstract Algebra, 7th ed., Pearson Ed.

2. Devi Prasad : Elementary Linear Algebra : Narosa.

Module I (30 hrs)

1. Binary operations

2. Isomorphic binary structures

3. Groups and subgroups - Sec. 2, 3, 4 and 5 of (1)

4. Groups of Permutations – Sec. 8 and 9 of (1)

5. Homomorphism – definition and simple examples – Sec. 13 of (1).

6. Rings and Fields – definition and simple examples.

Module II : Linear Algebra (24 hrs)

Vector space, subspace, linear dependence and independence.

Basis and dimension – simple examples

Linear transformations and matrix of linear transformations – simple examples

(Text 2)

References

1. Joseph A. Gallian: Contemporary Abstract Algebra – Narosa Pub. House.

2. K. Hoffman & R. Kunze : Linear Algebra – Pearson Education.

(For students not having Mathematics as Core Course)

MAT5D18: MATHEMATICS FOR NATURAL SCIENCES

3 hours/week **2 credits**

Text : Murray R. Spiegel : Statistics, 2nd Edn., Schaum's Outline Series.

Module I (30 hrs)

The idea of sets. Operation on sets. Relations and functions.

Variables and graphs (Chapter 1 of text 1).

Frequency distributions (Chapter 2 of text 1).

The Mean, Median, Mode and other measures of central tendency (Chapter 3 of text 1).

Dispersion or variation, The Range, The Mean deviation, The Semi-inter quartile range, Then 10-90 Percentile range; The standard deviation. Properties of standard deviation. The variance. Short methods of computing standard deviation (Relevant section of Chapter 4 of text 1).

Module II (24 hrs)

Moments, Moments for grouped data, relation between moments, Computation of moment for grouped data. Skewness and Kurtosis. (relevant sections of Chapter 5 from text 1).

Elements of Probability theory (Chapter 6 of text 1).

The Binomial distribution. The Normal distribution. Poisson distribution (Relevant sections from Chapter 7 of text 1)).

References

1. Hogg & Craig: Introduction to Mathematical Statistics.

2. Freund & Walpole: Mathematical Statistics.

(For students not having Mathematics as Core Course)

MAT5D19 : MATHEMATICS FOR SOCIAL SCIENCES

3 hours/week **2 credits**

Text Book: Edward T. Dowling : Calculus for Business, Economics and Social Sciences, Schaum's Outline Series, TMH, 2005.

Module I : Equations and Graphs (27 hrs)

2.1 Equations

2.2 Cartesian Coordinate System

2.3 Graphing linear equations

2.4 The slope of art line

2.5 Solving linear equations simultaneously

2.6 Solving quadratic equations

2.7 Practical applications

Functions

3.1 Concepts and definitions

32. Functions and graphs

3.3 The Algebra of Functions

3.4 Applications of linear functions

3.5 Facilitating non-linear graphs

3.6 Applications of non-linear functions

The derivative

4.1 Limits

4.2 Continuity

4.3 Slope of a Curvilinear function

4.4 Rates of change

4.5 The derivative

4.6 Differentiability and Continuity

4.7 Application

Differentiation 44

5.1 Derivative rotation

5.2 Rules of differentiation

5.3 Derivation of the rules of differentiation

5.4 Higher order derivatives

5.5 Higher order derivative notation

5.6 Implicit differentiation

5.7 Applications

Module II : Uses of Derivative (27 hrs)

6.1 Increasing and decreasing functions

6.2 Concavity

6.3 Extreme points

6.4 Inflexion points

6.5 Curve sketching

Exponential and Logarithmic functions

7.1 Exponential functions

7.2 Logarithmic functions

7.3 Properties of exponents and logarithms

7.4 Natural exponential and Logarithmic functions

7.5 Solving natural exponential and logarithmic functions.

7.6 Derivatives of natural exponential and logarithmic functions.

7.7 Logarithmic differentiation

7.8 Applications of exponential functions

7.9 Application of Logarithmic functions

Integration

8.1 Antidifferentiation

8.2 Rules for indefinite integrals

Multivariable Calculus

9.1 Functions of several variables

9.2 Partial derivatives

9.3 Rules of partial differentiation

9.4 Second order partial derivatives

More of Integration

10.1 Integration by substitution

10.2 Integration by parts

References

1. Srinath Baruah : Basic Mathematics and its Applications in Economics, Macmillan.

2. Taro Yamane: Mathematics for Economists, Second ed., PHI.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (COMPLEMENTARY COURSE)

B.Sc. DEGREE PROGRAMME

MATHEMATICS (COMPLEMENTARY COURSE)

FIRST SEMESTER

MAT 1C01 : MATHEMATICS

4 hours/week **3 credits**

Text : George B. Thomas Jr. and Ross L. Finney : Calculus, LPE, Ninth edition, Pearson Education.

Module I (20 hrs)

Limits and Continuity: Rules for finding limits. Target values and formal definitions of limits. Extensions of limit concept, Continuity, Tangent lines (Section 1.2, 1.3, 1.4, 1.5 & 1.6 of the Text).

Module II (12 hrs)

Derivatives: The derivative of a function, a quick review of differentiation rules, rate of change. (Section 2.1, 2.2, 2.3 of the Text)

Module III (24 hrs)

Application of derivatives: Extreme values of a function. The mean value theorem, First derivative test, Graphing with y' and y". Limits as $x \to \pm \infty$.Asymptotes and Dominant terms, Linearization and differentials.(Section 3.1, 3.2, 3.3, 3.4, 3.5, 3.7 of the Text). The L'Hopital's Rule (See section 6.6 of the Text).

Module IV (16hrs)

Integration: Riemann sums and Definite integrals; properties, areas and the Mean value theorem. The Fundamental theorem. (Section 4.5, 4.6, 4.7 of the Text).

Application of Integrals: Areas between curves, Finding Volumes by slicing. (Section 5.1, 5.2 of the Text.)

References

1. S.S. Sastry, Engineering Mathematics, Volume 1, 4th Edition PHI.

2. Muray R Spiegel, Advanced Calculus, Schaum's Outline series.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (COMPLEMENTARY COURSE)

SECOND SEMESTER

MAT2C02 : MATHEMATICS

4 hours/week **3 credits**

Text: George B Thomas, Jr and Ross L Finney: CALCULUS, LPE, Ninth edition, Pearson Education.

Module I: Hyperbolic functions, Application of Integrals and Improper Integrals, (20 hrs)

Hyperbolic Functions- Definitions and Identities, Derivatives and Integrals, Inverse Hyperbolic Functions- Derivatives and Integrals.

Application of Integrals :, Volumes of Solids of Revolution (Disk method only), Lengths of plane curves. Areas of surfaces of revolution

Improper Integrals- Convergence and Divergence, Tests for Convergence and Divergence- Direct Comparison Test and Limit Comparison Test

(Section: 5.3, 5.5, 5.6 , 6.10 & 7.6 of the Text)

ModuleII: Infinite Series (28 hrs)

Limit of Sequences of Number, Theorems for calculating limits of sequences (Excluding Picard's Method), Infinite series, The ratio and root test for series of non negative terms, Alternating series, Absolute and conditional convergence, Power Series, Taylor and Maclaurin Series.

(Sections 8.1, 8.2, 8.3, 8.6, 8.7, 8.8, 8.9 of the Text)

Module III : Polar Coordinates (10 hrs)

Polar coordinates, Graphing in Polar Coordinates, Polar equations for conic sections, Integration in Polar coordinates, Cylindrical and Spherical Coordinates.

(Sections 9.6, 9.7, 9.8, 9.9, 10.7 of the Text)

Module IV : Multivariable Functions and Partial Derivatives (14 hrs)

Functions of Several Variables, Limits and Continuity, Partial Derivatives, differentiability, Chain rule (Sections 12.1, 12.2, 12.3, 12.4, 12.5 of the Text)

References

1. S.S. Sastry, Engineering Mathematics, Volume I & II, 4th Edition PHI.

2. Murray R. Spiegel, Advanced Calculus, Schaum's Outline Series.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (COMPLEMENTARY COURSE)

THIRD SEMESTER

MAT3C03 : MATHEMATICS

5 hours/week **3 credits**

Text :

1. Erwin Kreyszig : Advanced Engineering Mathematics, Eighth Edition, Wiley, India.
2. Frank Ayres JR : Matrices, Schaum's Outline Series, TMH Edition.

Module I : Ordinary Differential Equations (20 hrs)

Basic concepts and ideas, Geometrical meaning of $y' = f(x,y)$. Direction Fields, Separable Differential Equations. Exact Differential Equations; Integrating Factors, Linear Differential Equations; Bernoulli Equation, Orthogonal Trajectories of Curves.
(Sections 1.1, 1.2, 1.3, 1.5, 1.6, 1.8 of Text 1).

Module II : Matrices (20 hrs)

Rank of a Matrix, Non-Singular and Singular matrices, Elementary Transformations, Inverse of an elementary Transformations, Row Canonical form, Normal form.

Systems of Linear equations: Homogeneous and Non Homogenoeus Equations, Characteristic equation of a matrix; Characteristic roots and characteristic vectors. Cayley-Hamilton Theorem (statement only) and simple applications (relevant sections of Text 2).

Module III : Vector Differential Calculus (25 hrs)

A quick Review of vector algebra, Inner product and vector product in R^2 and R^3.Vector and scalar functions and Fields, Derivatives, Curves, Tangents, Arc Length, Velocity and acceleration, Gradient of a scalar field; Directional Derivative, Divergence of a vector field, Curl of a Vector Field.
(Sections 8.1, 8.2, 8.3, 8.4, 8.5, 8.6, 8.9, 8.10, 8.11 of Text 1).

Module IV : Vector Integral Calculus (25 hrs)

Line Integrals, Independence of path, Green's Theorem in the Plane (without proof), surfaces for Surface Integrals, Surface Integrals, Triple Integrals, Divergence theorem of Gauss and Stoke's theorem (without proofs).
(Sections 9.1, 9.2, 9.4, 9.5, 9.6, 9.7, 9.9, 9.10 of Text 1)

References :

1. S.S. Sastry, Engineering Mathematics, Volume II, 4th ed., PHI.
2. Shanthi Narayanan & P.K. Mittal, A Text Book of Matrices, S. Chand.
3. Harry F. Davis & Arthur David Snider, Introduction to Vector Analysis, 6th ed., Universal Book Stall, New Delhi.
4. Murray R. Spiegel, Vector Analysis, Schaum's Outline Series, Asian Student edition.

B.Sc. DEGREE PROGRAMME

MATHEMATICS (COMPLEMENTARY COURSE)

FOURTH SEMESTER

MAT4C04 : MATHEMATICS

5 hours/week **3 credits**

Texts:

1. Erwin Kreyszig, Advanced Engineering Mathematics, Eighth Edition, Wiley, India.

2. George B. Thomas, Jr. and Ross L. Finney, Calculus, LPE, Ninth Edition, Pearson Education.

Module I: Linear Differential equations of Second and Higher order (20hrs)

Linear Differential equations of Second and Higher order: Differential Operators, Euler-Cauchy Equation, Wronskian, Nonhomogeneous Equations, Solutions by Undetermined Coefficients, Solution by variation of Parameters.

(Sections 2.1, 2.2, 2.3, 2.4, 2.6, 2.7, 2.8, 2.9, 2.10 of Text 1).

Module II: Laplace Transforms (20 hrs)

Laplace Transforms: Laplace Transform, Inverse Transform, Linearity, Shifting, Transforms of Derivatives of Integrals, Differential Equations. Unit step Function, Second Shifting Theorem, Dirac Delta Function, Differentiation and integration of Transforms, Convolution, Integral Equations, Partial Fractions, Differential Equations.
(Sections 5.1, 5.2, 5.3, 5.4, 5.5, 5.6 of Text 1 – excluding Proofs).

Module III : Fourier Series ,Partial differential Equations(30 hrs)

Fourier Series : Periodic Functions, Trigonometric Series, Fourier Series, Even and Odd functions, Half-range Expansions.
(Sections 10.1, 10.2, 10.4 of Text 1 – Excluding Proofs).

Partial differential Equations: Basic Concepts, Vibrating String, Wave Equation, Separation of Variables, Use of Fourier Series.
(sections 11.1, 11.2, 11.3 of Text 1).

Module IV: Numerical Methods (20 hrs)

Numerical Methods: Methods of First-order Differential Equations (Section 19.1 of Text 1).
Picard's iteration for initial Value Problems.(Section 1.9 of Text 1).

Numerical Integration: Trapezoidal Rule, Simpson's Rule. (Section 4.9 of Text 2).

References:

1.S.S. Sastry, Engineering Mathematics, Vol. II, 4th ed., PHI.
2. Murray R. Spiegel, Advanced Calculus, Schaum's Outline Series.
3. Murray R. Spiegel, Laplace Transforms, Schaum's Outline Series.